

# Regularized Nonparametric Estimation of Ill-posed Games of Incomplete Information

## WORK IN PROGRESS

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### Abstract

We want to estimate nonparametrically ill-posed games of incomplete information. The problem is studied in the form of an inverse problem, more precisely a nonlinear inverse problem. Typically, the functional form to recover is the distribution of the players private information. Our model can be written as  $T(F) = G$ , where  $F$  is the distribution of interest,  $G$  the identified distribution of observable actions and  $T$  a nonlinear operator. It is an ill-posed inverse problem if we cannot find a solution  $F$  that is unique and stable. In other words, we cannot find a continuous inverse operator  $T^{-1}$  in order to obtain a solution  $F$ . In general, it is possible to solve our nonlinear ill-posed inverse problem and estimate nonparametrically  $F$ . However, we show that estimating instead the quantile function  $F^{-1}$  allow us to linearise our inverse problem and derive convergence and asymptotic normality.